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UNITED STATES PATENT APPLICATION

FOR

**ACCELERATED HANDWRITTEN
SYMBOL RECOGNITION IN A PEN
BASED TABLET COMPUTER**

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FEDERAL SUPPORT STATEMENT

The present application is based on U.S. provisional patent application No. 60/201,581 filed on May 3, 2000, and claim priority to that application.

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BACKGROUND OF THE INVENTION

1. FIELD OF THE INVENTION

10 The present invention relates to the field of image recognition, and in particular to a method and apparatus for accelerated handwritten symbol recognition in a pen based tablet computer.

2. BACKGROUND ART

15 In some computer systems, handwritten symbols are input to the system. These symbols are translated by the computer system to machine readable characters. This translation is typically computation intensive. In some computer systems, battery operated portable devices for example, the general purpose central processing unit (CPU)
20 used for the translation is inefficient in its power consumption during the translation operation. Thus, the battery is drained more rapidly. Additionally, some battery operated systems are limited in computational power. When a real-time translation requirement is placed on symbol translation, the limited computational power results in a limited degree of accuracy in the translation process. These problems can be better understood with a
25 review of handwritten data entry.

Handwritten Data Entry

A typical computer system consists of a central processing unit (CPU), main
5 memory such as random access memory (RAM), a data entry device, including a
positioning device, a mass storage device such as one or more disk drives, a display
and/or a printer. In the prior art, the data entry device often consists of a keyboard, on
which a user enters data by typing. The positioning device of a prior art computer system
may consist of a "mouse" or other cursor positioning device.

10 Computer systems also exist that are directed to handwritten data entry rather than
keyboard data entry. These systems are often characterized by the use of a pen, stylus, or
other writing device, to enter handwritten data directly on the display of the computer
system. Alternatively, these systems may provide for a user to enter data on a digitizing
15 tablet or other input device, with the image of the written input displayed on a separate
computer display output device. The writing device for entering handwritten or freestyle
stroke input information is not limited to a pen or stylus, but may be any input device
such as a mouse, trackball, pointer, or even a person's fingers. Such systems are not
necessarily limited to receiving data generated by human users. For example, machine
20 generated data may also be inputted and accepted to such systems.

One class of this handwriting entry computer system that receives handwritten
data input is referred to as a "pen based" computer system. In a pen based computer
system, a writer can input information on a display by "writing" directly on the display. A
25 writing device, such as a pen or stylus, is used to enter information on the display. In a

typical pen-based computer system, a user touches the stylus to the display and writes as the user would on a piece of paper, by making a series of pen strokes to form letters and words. A line appears on the display that follows the path of travel of the pen point, so that the pen strokes appear on the display as ink would appear on a handwritten page.

- 5 Thus, the user can enter information into the computer by writing on the display. Pen based computers typically have a display surface that serves as both an input receiving device and as an output display device.

Handwritten Data Translation

10 One characteristic of handwriting entry computer systems is the ability to translate original handwritten symbols into machine readable words or characters for display. This translation is accomplished via a "character recognition" algorithm. The handwritten symbols are translated into, for example, ASCII characters. After the translation, the appearance of the displayed characters is as if they had been typed in via a keyboard.

To translate a handwritten character into a machine readable character, the handwritten character is compared to a library of characters to determine if there is a match. A description, or "template" for each character is defined and stored in memory.

- 20 Handwritten characters are compared to the stored templates. Match coefficients, reflecting how closely a handwritten character matches the template of a stored character, are calculated for each template character. The template character with the highest match coefficient is identified. The character represented by this template provides the "best fit" for the handwritten character. If the match coefficient for the "best fit" character exceeds
- 25 a predetermined minimum threshold, the "best fit" character is adopted. If the match

coefficient for the "best fit" character is less than the minimum threshold value, no translation is done. If the handwritten character cannot be translated, the character must be re-entered.

- 5 A disadvantage of current character recognition algorithms is limited accuracy. Often, handwritten characters are not translated at all or are mistranslated as an ASCII character other than the handwritten character. The mistranslated character must then be rewritten by the user, sometimes repeatedly, until a correct translation is made.

10 Handwriting Recognition in Portable Systems

- 15 A portable pen-based computer systems is constrained by the amount of power stored in its battery. Typically, portable pen-based computer systems, which require handwriting recognition (HWR), rely on grid based single character recognition, which forces users to print characters in stylized formats. This approach is not suitable for entering large text segments. A better approach for entering large text segments is to enable users to write naturally on the screen in their own personal, unconstructed style using HWR algorithms. However, HWR algorithms require a large amount of computation to translate handwritten symbols into machine readable characters. Typical portable pen-based computer systems lack the computational power necessary to satisfactorily perform translations.
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- Typical portable pen-based computer systems use a general purpose CPU for HWR calculations. Typically, a general purpose CPU is inefficient in power consumption during HWR calculations. The general purpose CPU is designed to perform
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more than HWR calculations, so some functions of the CPU are powered, but not used for the HWR calculation. Additionally, a general purpose CPU is inefficient in speed during HWR calculations. The general purpose CPU must be able to perform certain operating system tasks while completing HWR calculations. Thus, the speed with which HWR calculations are completed is diminished. As a result, fewer HWR calculations may be completed in a limited amount of time. Thus, if the time for HWR is limited, the accuracy of the translation is also limited.

Single Symbol Translation

Typically, portable pen-based computer systems translate one character at a time. However, such a scheme is difficult when a user has poor handwriting. For example, Figure 1 illustrates a word where single symbol translation is difficult. A single symbol translation system has difficulty translating the letters "m" (100), "i" (110), and "n" (120) in the word "jumping" (130) in Figure 1. However, the word is legible to the user.

SUMMARY OF THE INVENTION

The present invention provides a method and apparatus for accelerated handwritten symbol recognition in a pen based tablet computer. In one embodiment, handwritten symbols are translated into machine readable characters using hidden Markov models. In one embodiment, handwritten symbols are translated into machine readable characters using special purpose hardware. In one embodiment, the special purpose hardware is a recognition processing unit (RPU) which performs feature extraction and recognition. A user inputs the handwritten symbols and software recognition engine preprocesses the input to a reduced form. In one embodiment, the preprocessor is fully information preserving.

The data from the preprocessor is sent to the RPU which performs feature extraction and recognition. In one embodiment, the RPU has memory and the RPU operates on data in its memory. In one embodiment, the RPU uses a hidden Markov model (HMM) as a finite state machine that assigns probabilities to a symbol state based on the preprocessed data from the handwritten symbol. In another embodiment, the RPU recognizes collections of symbols, termed "wordlets," in addition to individual symbols.

In one embodiment, the software recognition engine uses the data from the RPU in a postprocessor. The postprocessor computes a stream of symbol observation events from data produced by the RPU and writer confirmation data. In one embodiment, the postprocessor also uses information about context, spelling, grammar, past word usage and user information to improve the accuracy of the symbols produced.

BRIEF DESCRIPTION OF THE DRAWINGS

These and other features, aspects and advantages of the present invention will become better understood with regard to the following description, appended claims and
5 accompanying drawings where:

Figure 1 is a block diagram of a word where single symbol translation is difficult.

10 Figure 2 is a block diagram of a pen-based (tablet) computer handwriting symbol recognition system in accordance with one embodiment of the present invention.

Figure 3 is a flow diagram of the process of translating handwritten symbols in accordance with one embodiment of the present invention.

15 Figure 4 is a flow diagram of the process of translating handwritten symbols wherein the RPU calculates forward and backward probabilities in accordance with one embodiment of the present invention.

20 Figure 5 is a flow diagram of the process of translating handwritten symbols wherein the RPU calculates forward probabilities in accordance with one embodiment of the present invention.

Figure 6 is a block diagram of an RPU in accordance with one embodiment of the present invention.

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Figure 7 is a flow diagram of the process of handwritten symbol translation using context information in accordance with one embodiment of the present invention.

5 Figure 8 is a flow diagram of the process of handwritten symbol translation using spelling information in accordance with one embodiment of the present invention.

Figure 9 is a flow diagram of the process of handwritten symbol translation using grammar information in accordance with one embodiment of the present invention.

10 Figure 10 is a flow diagram of the process of handwritten symbol translation using past word usage information in accordance with one embodiment of the present invention.

15 Figure 11 is a flow diagram of the process of handwritten symbol translation using user information in accordance with one embodiment of the present invention.

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DETAILED DESCRIPTION OF THE INVENTION

The invention is a method and apparatus for accelerated handwritten symbol recognition in a pen based tablet computer. In the following description, numerous specific details are set forth to provide a more thorough description of embodiments of the invention. It is apparent, however, to one skilled in the art, that the invention may be practiced without these specific details. In other instances, well known features have not been described in detail so as not to obscure the invention.

Handwriting Recognition Calculations

In one embodiment, HMM calculations are used to determine the probability of a symbol appearing in a sequence of symbol observations. A HMM with N states, M observation symbols, the state alphabet $V_s = \{S_1, S_2, \dots, S_N\}$ and the emission alphabet $V_e = \{v_1, v_2, \dots, v_M\}$ is defined by the triplet $\lambda = (A, B, \pi)$. A is a state transition matrix defined as $a_{ij} = P(q_{t+1} = S_j \mid q_t = S_i)$ for $1 \leq i \leq N$ and $1 \leq j \leq N$, which means the probability that the state at time $t+1$ is state j given that the state at time t is state i . B is the observation probability matrix defined as $b_j(k) = P(v_k \mid q_t = S_j)$ for $1 \leq j \leq N$ and $1 \leq k \leq M$, which means the probability of the observation being v_k given that the state at time t is state j . p is an initial state distribution defined as $\pi_i = P(q_1 = S_i)$, which means the probability of the state at time 1 is state i .

If we have an observation sequence $O = (o_1 o_2 \dots o_T)$, the RPU calculates the probability of this sequence given the model λ . This value is calculated by determining a series of values termed forward variables defined as $\alpha_i(t) = P(o_1 o_2 \dots o_t, q_t = S_i \mid \lambda)$, which

means the probability of the observation sequence from 1 to t and the state at time t being state i given λ . These values are calculated by initializing the variable as $\alpha_i(1) = \pi_i b_i(o_1)$ for $1 \leq i \leq N$. Further values are calculated using $\alpha_j(t+1) = b_j(o_{t+1}) \sum_{i=1}^N \alpha_i(t) a_{ij}$ for

1 $1 \leq t \leq T-1$ and $1 \leq j \leq N$. The probability of the sequence given λ is defined by $P(P | \lambda) = \sum_{i=1}^N \alpha_i(T)$.

Similarly, a backward variable is defined as $\beta_i(t) = P(o_{t+1} o_{t+2} \dots o_T | q_t = S_i, \lambda)$, which means the probability of the observation sequence from t+1 to T given state at time t being state i given λ . The backward variables are initialized as $\beta_i(T) = 1$ for $1 \leq i \leq N$. Further values are calculated using $\beta_j(t) = \sum_{i=1}^N a_{ij} b_j(o_{t+1}) \beta_i(t+1)$ for $1 \leq t \leq T-1$ and $1 \leq j \leq N$.

The calculations to compute forward and backward variables are performed in the RPU. Thus, probabilities can be calculated for each new symbol to determine which symbols the new symbol is most likely to be. In one embodiment, the HMM calculations are performed on a general purpose computational unit.

Pre-processed symbol observations are the input to the HMMs. In one embodiment, the symbol observation alphabet (the emission alphabet) is comprised of angles of equalized segments. In other embodiment, more complex symbol observation alphabets are used. In one embodiment, at least one HMM is created for each symbol in the output alphabet. The probability of each symbol given the observation sequence is calculated by each symbol's HMM. In one embodiment, a post-processing unit uses the information from the HMMs to determine the appropriate symbol.

Training A, B and π

It is desirable to select the parameters A, B and π of λ that maximize the probability of a sequence in the training set given λ . One algorithm used to determine the parameters is the Baum-Welch method. The Baum-Welch method guarantees a monotonically increasing probability and converges quickly.

First, a joint event variable is defined as $\epsilon_{ij}(t) = P(q_t = S_i, q_{t+1} = S_j \mid O, \lambda)$, which means that the probability of the state at time t being state i and the state at time $t+1$ being state j given sequence O and λ . From the definitions of forward and backward variables, this becomes $\epsilon_{ij}(t) = (\alpha_i(t)a_{ij}b_j(o_{t+1})\beta_j(t+1)) / P(O \mid \lambda)$.

Additionally, a state variable is defined as $\gamma_i(t) = P(q_t = S_i \mid O, \lambda)$, which means the probability of the state at time t being state i given sequence O and λ . From the definitions of forward and backward variables, this becomes $\gamma_i(t) = (\alpha_i(t)\beta_i(t)) / P(O \mid \lambda)$.

A new λ, λ' , is calculated as follows. A new a, a' , is calculated as $a'_{ij} = \frac{\sum_{t=1}^{T-1} \epsilon_{ij}(t)}{\sum_{t=1}^{T-1} \gamma_i(t)}$. A new b, b' , is calculated as $b'_j = \frac{\sum_{t=1, o_t=v_k}^T \gamma_j(t)}{\sum_{t=1}^T \gamma_j(t)}$. A new π, π' , is calculated as $\pi'_i = \gamma_i(1)$.

A variation of the Baum-Welch method, termed the "Levingson method," calculates λ' as follows when K observation sequences are used to adjust the parameters. A new a, a' , is calculated as $a'_{ij} = \frac{\sum_{k=1}^K \sum_{t=1}^{T-1} \epsilon_{ij}^{(k)}(t)}{\sum_{k=1}^K \sum_{t=1}^{T-1} \gamma_i^{(k)}(t)}$. A new b, b' , is

calculated as $b_j^{(k)} = \sum_{k=1}^K \sum_{t=1, o_t=v_k}^T \gamma_j^{(k)}(t) / \sum_{k=1}^K \sum_{t=1}^T \gamma_j^{(k)}(t)$. A new π, π' , is calculated as $\pi'_i = 1/K * \sum_{k=1}^K \gamma_i^{(k)}(1)$.

Special Purpose Hardware for Recognition Processing

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In one embodiment, handwritten symbols are translated into machine readable characters using special purpose hardware. In one embodiment, the special purpose hardware is a recognition processing unit (RPU) which performs feature extraction and recognition. In another embodiment, a user inputs the handwritten symbols and software recognition engine preprocesses the input to a reduced form. In one embodiment, the preprocessor is fully information preserving.

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Figure 2 illustrates a pen-based (tablet) computer handwriting symbol recognition system in accordance with one embodiment of the present invention. A writer (200) enters handwritten symbols into the tablet computer (210). The handwritten symbols operated upon by a preprocessor (220) running on the main processing unit (MPU). The data from the preprocessor is sent to an RPU (230). The RPU is implemented as special-purpose hardware. In one embodiment, the RPU is a circuit configured to perform hidden Markov model (HMM) computations. The data from the RPU is used by a postprocessor (240) running on the MPU to produce an unconfirmed symbol observation (250).

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The unconfirmed symbol observation is presented to the writer. The writer can confirm a symbol, reject a symbol or make no determination. The postprocessor uses confirmed symbol observations (260), rejected symbol observations and unconfirmed

symbol observations to adjust how it makes symbol observations. The preprocessor also uses confirmed symbol observations and unconfirmed symbol observations to adjust how it preprocesses the handwritten symbols. Additionally, training data (270) is used by the preprocessor, the RPU, and the postprocessor to adjust their calculation to achieve more accurate symbol translations.

The special purpose hardware of the RPU enables the system to calculate more handwriting recognition calculations in the same amount of time when compared to a system where handwriting recognition calculations are performed by a general purpose processor (the MPU). In one embodiment, the RPU uses parallel processing to make multiple handwriting recognition calculations each clock cycle. Typically, a general purpose processor requires multiple clock cycles to perform one handwriting recognition calculation. In one embodiment, the RPU performs eight handwriting recognition calculations in parallel for each clock cycle. Since the RPU only performs handwriting recognition calculations, no power is wasted during the calculation. Thus, the same amount of handwriting recognition calculations will require less power when computed by an RPU than when computed by a general purpose processor.

Memory on the RPU

In one embodiment, the data from the preprocessor is sent to the RPU which performs feature extraction and recognition. In another embodiment, the RPU has memory and the RPU operates on data in its memory. Figure 3 illustrates the process of translating handwritten symbols in accordance with one embodiment of the present invention. At step 300, a user enters handwritten symbols into the system. At step 310,

the handwritten symbol data is stored in memory accessible by the MPU. At step 320, a preprocessor running on the MPU operates on the handwritten symbols. At step 330, the data from the preprocessor is transferred to the memory of an RPU. At step 340, the RPU operates on the data in its memory. At step 350, the data from the RPU is transferred to the memory accessible by the MPU. At step 360, a postprocessor running on the MPU generates a symbol observation.

Figure 4 illustrates the process of translating handwritten symbols wherein the RPU calculates forward and backward probabilities in accordance with one embodiment of the present invention. At step 400, a user enters handwritten symbols into the system. At step 410, the handwritten symbol data is stored in memory accessible by the MPU. At step 420, a preprocessor running on the MPU operates on the handwritten symbols. At step 430, the data from the preprocessor is transferred to the memory of an RPU. At step 440, the RPU calculates forward and backward probabilities. At step 450, the data from the RPU is transferred to the memory accessible by the MPU. At step 460, a postprocessor running on the MPU generates a symbol observation.

Figure 5 illustrates the process of translating handwritten symbols wherein the RPU calculates forward probabilities in accordance with one embodiment of the present invention. At step 500, a user enters handwritten symbols into the system. At step 505, the handwritten symbol data is stored in memory accessible by the MPU. At step 510, a preprocessor running on the MPU operates on the handwritten symbols. At step 515, the data from the preprocessor is transferred to the memory of an RPU. At step 520, the RPU calculates initial forward probabilities, $\alpha_i(1)$. At step 525, the RPU calculates successive forward probabilities ($\alpha_i(2)$, $\alpha_i(3)$, ..., $\alpha_i(t)$) to determine the probabilities of the observed

sequences. At step 530, the data from the RPU is transferred to the memory accessible by the MPU. At step 535, a postprocessor running on the MPU generates a symbol observation.

Figure 6 illustrates an RPU in accordance with one embodiment of the present invention. The RPU 600 has a memory unit 610 which stores a_{ij} 620, $b_i(o_{t+1})$ 630 and values of $\alpha_i(t)$ 640 as they are calculated. Initially, the values of $\alpha_i(t)$ are set to their initial values. Additionally, the RPU has a HMM calculation unit 650. The HMM has N $\alpha_i(t)$ units 660. Each $\alpha_i(t)$ unit is multiplied by the appropriate a_{ij} value in an a_{ij} unit 670. All of the products are summed in a summation unit 680 and the sum is multiplied by the appropriate $b_i(o_{t+1})$ value stored in a $b_i(o_{t+1})$ unit 690. The resulting product is stored in the memory unit. Thus, the HMM calculates $\alpha_j(t+1) = b_i(o_{t+1}) \sum_{i=1}^N \alpha_i(t) a_{ij}$ for $1 \leq t \leq T-1$ and $1 \leq j \leq N$.

In some embodiments, the RPU has multiple HMM calculation units to enable multiple HMM calculations to take place in parallel. In one embodiment, the RPU has N HMM calculation units. Thus, values of $\alpha_j(t+1)$ are calculated in parallel for all values of j .

Symbols and Wordlets

In one embodiment, the RPU uses a hidden Markov model (HMM) as a finite state machine that assigns probabilities to a symbol based on the preprocessed data from the handwritten symbol. For example, a handwritten symbol may have a one in three probability of being an “e” and a one in four probability of being an “i.” In another

embodiment, the RPU recognizes collections of symbols, termed "wordlets," in addition to individual symbols.

For example, the RPU may recognize "tion" or "ing" as one symbol. The output alphabet contains "tion" and "ing" in addition to "t", "i", "o", "n" and "g". The ability to recognize a handwritten symbol as the wordlet "ing" improves the accuracy of translation. For example, in Figure 1, the "i," the "n" and the "g" are all difficult to recognize individually. However, the "ing," together, is easier to recognize. Where one letter ends and the next begins becomes less important to the determination when the entire wordlet can be recognized by the RPU.

Probabilistic Context Free Grammar

In one embodiment, probabilistic context free grammar information is used to improve the accuracy of symbol translation. A probabilistic context free grammar is defined as $G = (V_N, V_T, P, S)$. V_N is a nonterminal feature alphabet defined as $V_N = \{F_1, F_2, \dots, F_N\}$. V_T is a terminal feature alphabet defined as $V_T = \{w_1, w_2, \dots, w_M\}$. All of the production rules of the grammar are of the form $F_i \rightarrow F_j F_k$ or $F_i \rightarrow w_k$ where $F_i \in V_N$ are nonterminal features and $w_k \in V_T$ are terminal features. F_1 is set equal to the entire string of terminals.

These production rules are defined by tensors A and B as $P = (A, B)$. For the nonterminal features, a probability tensor A of rank 3 is defined as $a_{ijk} = P(F_i \rightarrow F_j F_k)$ for $1 \leq i \leq N$, $1 \leq j \leq N$ and $1 \leq k \leq N$. For the terminal features, a production probability matrix B is defined as $b_j(k) = P(F_j \rightarrow w_k)$ for $1 \leq j \leq N$ and $1 \leq k \leq M$.

In one embodiment, the probability of a string of terminals of length T , $W = w^1 w^2 \dots w^T$, where $w^k \in V_T$ is determined given a probabilistic context free grammar defined as $P(W | G)$. In one embodiment, the probability of a sub-sequence, $W^{p,q} = w^p \dots w^q$, termed an “inside probability” is calculated. The inside probability is initialized as $\beta_i(t, t) = b_i(w^t)$ for $1 \leq i \leq N$ and $1 \leq t \leq T$. Successive inside probabilities are determined by calculating $\beta_i(p, q) = \sum_{j=1}^N \sum_{k=1}^N a_{ijk} \sum_{t=p}^{q-1} \beta_i(p, t) \beta_k(t+1, q)$ for $1 \leq i \leq N$. At termination, $P(W | G) = \beta_1(1, T)$.

Similarly, the “outside probability” is the probability that the sub-sequence, $W^{p,q} = w^p \dots w^q$, was generated by the nonterminal F_i in the sequence $W = w^1 w^2 \dots w^T$. The outside probability is initialized as $\alpha_i(1, T) = \delta_{1i}$ for $1 \leq i \leq N$. $\delta_{1i} = 1$ for $i = 1$ and $\delta_{1i} = 0$ for all other values of i . Successive outside probabilities are determined by calculating $\alpha_j(p, q) = \sum_{i=1}^N \sum_{k=1, j \neq k}^N a_{ijk} \sum_{t=q+1}^T \alpha_i(p, t) \beta_k(q+1, t) + \sum_{i=1}^N \sum_{k=1}^N a_{ijk} \sum_{t=1}^{p-1} \alpha_k(t, q) \beta_i(t, p-1)$ for $1 \leq j \leq N$. At termination, $P(W | G) = \sum_{j=1}^N b_j(w^1) \alpha_j(1, 1)$ for $1 \leq t \leq T$.

Training for Probabilistic Context Free Grammar

A joint feature probability is defined as $\xi_{ijk}(p, q) = \frac{\alpha_i(p, q) a_{ijk} \sum_{t=p}^{q-1} \beta_j(p, t) \beta_k(t+1, q)}{\beta_i(1, T)}$. A parent feature probability is defined as $\gamma_i(p, q) = \frac{\alpha_i(p, q) \beta_i(p, q)}{\beta_i(1, T)}$. The joint feature probability and parent feature probability are used to

calculate new nonterminal probabilities and new terminal probabilities. The new

nonterminal probabilities are calculated as $\bar{a}_{ijk} = \frac{\sum_{p=1}^{T-1} \sum_{q=p}^T \xi_{ijk}(p, q)}{\sum_{p=1}^T \sum_{q=p}^T \gamma_i(p, q)}$ for $1 \leq j \leq N$ and

$1 \leq k \leq M$. The new terminal probabilities are calculated as $\bar{b}_j(k) = \frac{\sum_{t=1, w'=w_k}^T \gamma_j(t, t)}{\sum_{p=1}^T \sum_{q=p}^T \gamma_j(p, q)}$ for

$1 \leq j \leq N$ and $1 \leq k \leq M$.

- 5 In one embodiment, the inside probability is used to determine a probability of a string of observed terminals given a probabilistic context free grammar. In one embodiment, the tensors of the probability are trained on a sample language by calculating new terminal and nonterminal probabilities using the above equations. In one embodiment, the inside probability is calculated using general purpose hardware. In another embodiment, the inside probability is calculated using special purpose hardware.

Context Consideration to Improve Accuracy

- 15 In one embodiment, the software recognition engine uses the data from the RPU in a postprocessor. The postprocessor computes a stream of symbol observation events from data produced by the RPU and writer confirmation data. In one embodiment, the postprocessor also uses information about context, spelling, grammar, past word usage and user information to improve the accuracy of the symbols produced.

- 20 Figure 7 illustrates the process of handwritten symbol translation using context information in accordance with one embodiment of the present invention. At step 700, a

user enters handwritten symbols into the system. At step 710, a preprocessor running on the MPU operates on the handwritten symbols. At step 720, the RPU operates on the data in its memory. At step 730, postprocessor running on the MPU operates on the data to generate a symbol observation using the context of the handwritten symbol.

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In one embodiment, the postprocessor uses spelling information combined with previously generated symbols to determine the current symbol. Figure 8 illustrates the process of handwritten symbol translation using spelling information in accordance with one embodiment of the present invention. At step 800, a user enters handwritten symbols into the system. At step 810, a preprocessor running on the MPU operates on the handwritten symbols. At step 820, the RPU operates on the data in its memory. At step 830, postprocessor running on the MPU adjusts the probability of symbols based on whether the symbol, in combination with applicable previous symbols, would produce a correctly spelled word or word segment in the current context. At step 840, the postprocessor generates a symbol observation. For example, the postprocessor would assign a higher probability to a symbol following a “q” being a “u” rather than being “ei”.

In another embodiment, the postprocessor uses grammar information combined with previously generated symbols to determine the current symbol. Figure 9 illustrates the process of handwritten symbol translation using grammar information in accordance with one embodiment of the present invention. At step 900, a user enters handwritten symbols into the system. At step 910, a preprocessor running on the MPU operates on the handwritten symbols. At step 920, the RPU operates on the data in its memory. At step 930, postprocessor running on the MPU adjusts the probability of symbols based on whether the symbol, in combination with applicable previous symbols, would produce a

set of symbols which are not grammatically incorrectly in the current context. At step 940, the postprocessor generates a symbol observation. For example, a processor would give a higher probability to the symbol following "I am an inventor to" being an "o" than being a ".".

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In one embodiment, the postprocessor uses past word usage information combined with previously generated symbols to determine the current symbol. Figure 10 illustrates the process of handwritten symbol translation using past word usage information in accordance with one embodiment of the present invention. At step 1000, a user enters handwritten symbols into the system. At step 1010, a preprocessor running on the MPU operates on the handwritten symbols. At step 1020, the RPU operates on the data in its memory. At step 1030, postprocessor running on the MPU adjusts the probability of symbols based on whether the symbol, in combination with applicable previous symbols, would produce a word, or segment of a word, which was previously input to the system. At step 1040, the postprocessor generates a symbol observation.

In one embodiment, the postprocessor uses user information combined with previously generated symbols to determine the current symbol. Figure 11 illustrates the process of handwritten symbol translation using user information in accordance with one embodiment of the present invention. At step 1100, a user enters handwritten symbols into the system. At step 1110, a preprocessor running on the MPU operates on the handwritten symbols. At step 1120, the RPU operates on the data in its memory. At step 1130, postprocessor running on the MPU adjusts the probability of symbols to account for known user information. For example, the system may know the user writes "ful" in a

